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WEIGHTED NORM INEQUALITIES FOR THE g–LITTLEWOOD–PALEY OPERATORS ASSOCIATED WITH LAPLACE–BESSEL DIFFERENTIAL OPERATORS

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Abstract. In this work we define and study Poisson integral associated with Laplace-Bessel differential operators. We establish weighted inequalities with a general weight for the g-Littlewood-Paley functions and the commutator $g_{b,k}$ defined by (1.2) associated with Laplace Bessel differential operator.

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